The Shapes of Molecules

10.1 Lewis Structures of Polyatomic Species

- **Skeleton structure** – the connectivity of atoms in polyatomic species
  - **Central atom(s)** – usually the atom with the lower group number or higher period number (lowest *EN)*
    - Often written first in the formula – PCl_5, SO_3, …
    - Normally **H** is not a central atom
  - Polyatomic ions
    - The cation and the anion of an ionic compound are treated separately
    - Total number of valence **e⁻** is adjusted for the charge of the ion

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Rules for Writing Lewis Structures

1. Write the **skeleton structure** by placing a single bond (**e⁻** pair) between each bonded pair of atoms
2. Count the total number of valence electrons of all atoms, n_{tot} (correct for the charges of ions)
3. Count the number of remaining electrons, n_{rem} (total number of **e⁻** minus **e⁻** used in the skeleton structure as bonds)
4. Count the number of needed electrons, n_{need} (the **e⁻** needed to complete the octet (or duplet) structures of all atoms)

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5. If $n_{need} = n_{rem}$, add the remaining **e⁻** as lone pairs to complete the octets for all atoms, or

   If $n_{need} > n_{rem}$, add multiple bonds (1 bond for each deficient pair of **e⁻**) and complete the structure with lone pairs

Example: Write the Lewis structure of **H_2O**.
1. **O** is the central atom (can't be H)
   $\Rightarrow$ **H–O–H** (**4 e⁻** in the skeleton structure)
2. $n_{tot} = 1(H) + 6(O) + 1(H) = 8$
3. $n_{rem} = 8 - 4 = 4$
4. $n_{need} = 0(H) + 4(O) + 0(H) = 4$
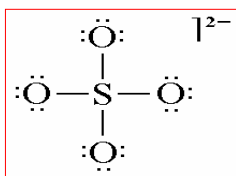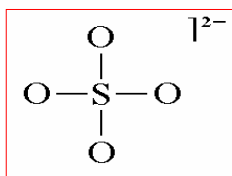5. $n_{need} = n_{rem}$ $\Rightarrow$ **H–Ö–H**

Example: Write the Lewis structure of **HCN**.
1. **C** is the central atom (lower group # than **N**)
   $\Rightarrow$ **H–C–N** (**4 e⁻** in the skeleton structure)
2. $n_{tot} = 1(H) + 4(C) + 5(N) = 10$
3. $n_{rem} = 10 - 4 = 6$
4. $n_{need} = 0(H) + 4(C) + 6(N) = 10$
5. $n_{need} > n_{rem}$ deficiency of **4 e⁻** (**2 e⁻** pairs)
   $\Rightarrow$ add **2** more bonds between **C** and **N** and complete the structure with lone pairs

   H–C≡N:
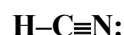
Example: Write the Lewis structure of **SO_4^{2-}**.
1. **S** is the central atom (higher period # than **O**)
   (**8 e⁻** in the skeleton structure)
2. $n_{tot} = 6(S) + 4 \times 6(O) + 2(charge) = 32$
3. $n_{rem} = 32 - 8 = 24$
4. $n_{need} = 0(S) + 4 \times 6(O) = 24$
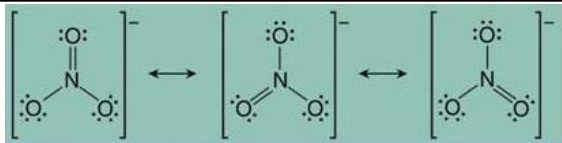5. $n_{need} = n_{rem} \Rightarrow$ complete structure with lone pairs

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Resonance in Lewis Structures

**Example:** Write the Lewis structure of **NO_3^-**.
1. **N** is the central atom (lower group # than **O**)
   6 e⁻ in the skeleton structure
2. $n_{tot} = 5(N) + 3 \times 6(O) + 1(charge) = 24$
3. $n_{rem} = 24 - 6 = 18$ 4. $n_{need} = 2(N) + 3 \times 6(O) = 20$
5. $n_{need} > n_{rem}$ deficiency of **2 e⁻** (**1 e⁻** pair)
   $\Rightarrow$ add **1** more bond between **N** and one of the **Os** and complete the structure with lone pairs
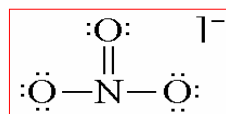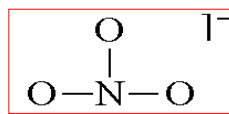
- All three structures are valid Lewis structures and differ by the position of bonds and lone pairs → **Resonance structures**
- Neither of the resonance structures is realistic
- The real structure is a blend (**resonance hybrid**) of the contributing Lewis structures
- The three bonds are identical (intermediate between a single and a double bond)
- The bond order is $(2+1+1)/3 = 1.33$

Example: Benzene, C_6H_6.
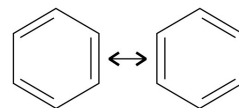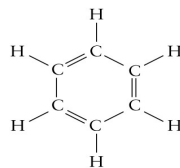
- The two structures have **equal energies** and **contribute equally** to the hybrid
- The electrons from the double bonds are **delocalized** between all six **C** atoms
- The six C–C bonds are identical with bond orders of 1.5

- **Formal charge (FC)** – a charge assigned to atoms in Lewis structures assuming that the shared e^- are divided equally between the bonded atoms.
  - The # of e^- assigned to an atom in a Lewis structure → all lone pair e^- (**L**) and half of the shared e^- (**S**)
  - The # of valence e^- of an atom (**V**) → V = group#
  - The # of bonds for an atom (**B**) → B = S/2

    $$FC = V - [L + S/2] = V - [L + B]$$

- The **FC** shows the extent to which atoms have gained or lost e^- in covalent bond formation
  - The sum of all **FC**s equals the charge of the species

Example: Write the possible resonance structures of the **NCO⁻** ion (N-C-O) including the formal charges of all atoms.

[N–C–O]⁻
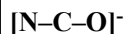
$n_{tot} = 5 + 4 + 6 + 1 = 16$

$n_{rem} = 16 - 4 = $ **12** $n_{need} = 6 + 4 + 6 = $ **16**

$n_{need} > n_{rem}$ deficiency of **4** e^- ⇒ add **2** more bonds

a) [:N̈=C=Ö:]⁻   b) [:N≡C–Ö̈:]⁻   c) [:N̈–C≡O:]⁻

V   →   5(N) 4(C) 6(O)

L+B → a) 6(N) 4(C) 6(O)   FC → a) -1(N)   0(C)   0(O)

L+B → b) 5(N) 4(C) 7(O)   FC → b) 0(N)   0(C)   -1(O)

L+B → c) 7(N) 4(C) 5(O)   FC → c) -2(N)   0(C)   +1(O)

- **FC**s are used to evaluate the relative importance of resonance structures
  1. Lewis structures with lower **FC**s are favored
  2. Lewis structures with like **FC**s on adjacent atoms are less favorable
  3. Lewis structures with negative **FC**s on the more electronegative atoms are favored

Example: Evaluate the importance of the three possible resonance structures of the **NCO⁻** ion

a) [:N̈=C=Ö:]⁻   b) [:N≡C–Ö̈:]⁻   c) [:N̈–C≡O:]⁻

   -1 0 0   0 0 -1   -2 0 +1
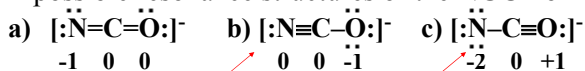
Most favored		Least favored
[(-) **FC** on the more **EN** atom]		(highest **FC**s)

Exceptions to the Octet Rule

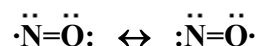- **Odd electron species** (radicals) → ·CH₃, ·OH, ·NO, ·NO₂, …
  - Have an unpaired electron – paramagnetic
  - Highly reactive and short lived species
  - Significance to atmospheric chemistry (smog) and human health (antioxidants)

Example: Write the Lewis structure of **NO**.

[N–O]

$n_{tot} = 5 + 6 = 11$ $n_{rem} = 11 - 2 = $ **9**

$n_{need} = 6 + 6 = $ **12**   ⇒ add **1** more bond

·N̈=Ö: ↔ :N̈=Ö·

• **Electron deficient molecules** – molecular compounds of some elements from groups 2 and 3A (**Be**, **B** and **Al**) form **incomplete octets** (have less than $8e^-$ around the central atom)

Example: Write the Lewis structure of BeH_2.

H–Be–H $\qquad$ $n_{tot} = 2 + 2\times1 = 4$

$n_{rem} = 4 - 4 = 0$ $\qquad$ $n_{need} = 4$

$\Rightarrow$ additional bonds can not be used (no remaining e^-)
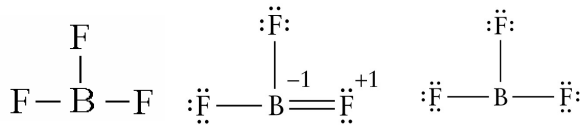
$$H–Be–H$$

$\Rightarrow$ the structure has an incomplete octet for the **Be** atom because the molecule is **electron-deficient**

Example: Write the Lewis structure of BF_3.
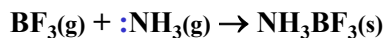
$n_{tot} = 3 + 3\times7 = 24$

$n_{rem} = 24 - 6 = 18$ $\qquad$ $n_{need} = 2 + 3\times6 = 20$

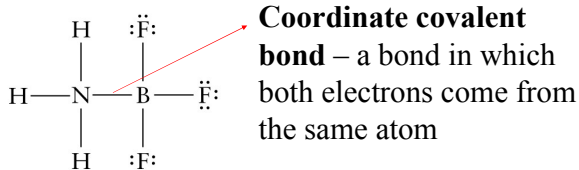$n_{need} > n_{rem}$ $\qquad$ deficiency of $2\ e^-$ $\Rightarrow$ add **1** more bond

The second resonance structure has only $6e^-$ around **B** (incomplete octet), but it is the favored structure due to the lower formal charges

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– Structures with incomplete octets are **electron-deficient** and tend to react with molecules that have abundance of e^- in the form of lone pairs

$$BF_3(g) + :NH_3(g) \rightarrow NH_3BF_3(s)$$

– The lone pair of **N** is used to form the bond between **B** and **N** and completes the octet of **B**

Coordinate covalent bond – a bond in which both electrons come from the same atom

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• **Expanded valence shells (extended octets)** – more than $8e^-$ around a central atom

– Extended octets are formed only by atoms with vacant **d**-orbitals in the valence shell (**p**-elements from the **third or later periods**)

– Extended octets form when:

• There are too many electrons ($n_{need} < n_{rem}$) or more than 4 atoms are bonded to the central atom – **electron-rich structures → place the extra electrons at the central atom**

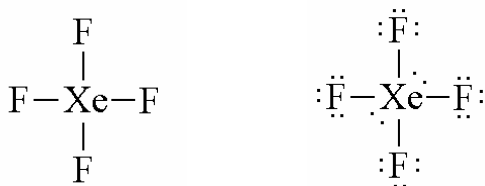• Structures with **lower formal charges** can be achieved by forming an extended octet

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Example: Write the Lewis structure of XeF_4.

$n_{tot} = 8(Xe) + 4\times7(F) = 36$

$n_{rem} = 36 - 8 = 28$ $\qquad$ $n_{need} = 0(Xe) + 4\times6(F) = 24$

$n_{need} < n_{rem}$

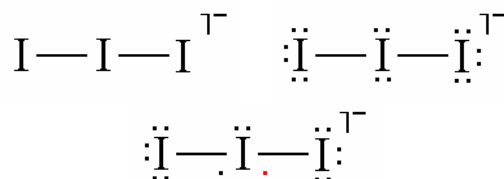4 extra e^- $\Rightarrow$ add **2** lone pairs at **Xe**

Example: Write the Lewis structure of I_3^-.
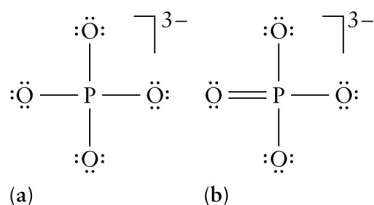
$n_{tot} = 3\times7(I) + 1(charge) = 22$

$n_{rem} = 22 - 4 = 18$ $\qquad$ $n_{need} = 4(I) + 2\times6(I) = 16$

$n_{need} < n_{rem}$ $\qquad$ **2** extra e^-

$\Rightarrow$ add **1** extra lone pair at the central **I** atom after completing the octets for all atoms

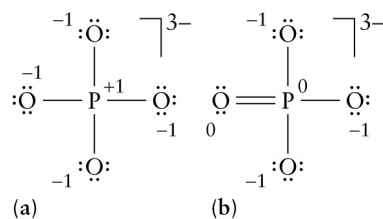**Example:** Select the favored resonance structure of the PO_4^{3-} anion.

Formal charges:
(a) O $\rightarrow$ 6-(6+1)=-1   P $\rightarrow$ 5-(0+4)=+1
(b) O– $\rightarrow$ 6-(6+1)=-1   P $\rightarrow$ 5-(0+5)=0
   O= $\rightarrow$ 6-(4+2)=0

(a)   (b)

– Structure (**b**) has an extended octet (10 e^-) at the **P** atom
– Structure (**b**) is more favored (contributes more to the resonance hybrid) due to the lower formal charges

# 9.4 Using Lewis Structures and Bond Energies to Calculate ΔH of Reaction

• Any reaction can be represented as a two step process in which:
  – All **reactant bonds break** to give individual atoms
  – All **product bonds form** from the individual atoms
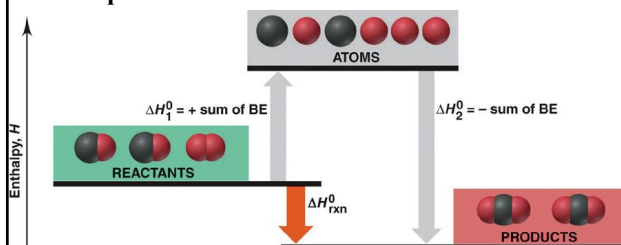
$\Rightarrow$ Average bond enthalpies can be used to estimate the enthalpy changes of reactions in the gas phase (only approximate values)

$$\Delta H_r^o = \Delta H_B(\text{broken}) - \Delta H_B(\text{formed})$$

– Energy is absorbed (+) to break the bonds of the reactants and emitted (-) during forming the bonds of the products
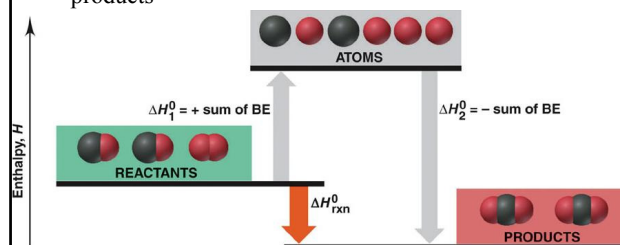
Example: Estimate the standard enthalpy of the reaction $CH_4(g) + 2F_2(g) \rightarrow CH_2F_2(g) + 2HF(g)$
1. Lewis structures are needed to get the bond order
2. Bonds broken (reactants):
   4 C–H (412 kJ/mol), 2 F–F (158 kJ/mol)
3. Bonds formed (products):
   2 C–H (412 kJ/mol), 2 C–F (484 kJ/mol), 2 H–F (565 kJ/mol)

$\Delta H^o = \Delta H_B(\text{broken}) - \Delta H_B(\text{formed})$ = [4×412 + 2×158] - [2×412 + 2×484 + 2×565] = -958 kJ

(this value is only an estimate, the exact value can be calculated using ΔH_f^o data)

10.2 Molecular Shape and the Valence-Shell Electron-Pair Repulsion Model

• The chemical and physical properties of compounds are intimately related to their molecular shapes
  – **Molecular shapes** (geometries) depend on the three-dimensional arrangement of atoms in space
    • Bond **distances**, bond **angles, …**
  – Lewis structures do not represent the true shape of molecules
  – Molecular shapes are studied experimentally, but can be predicted using various theoretical models

- **Valence-shell electron-pair repulsion (VSEPR) model** – the electron-groups around a central atom are arranged as far from one another as possible in order to minimize the repulsion between them
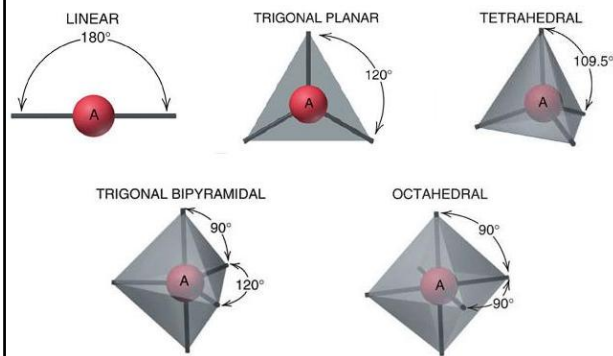 - **Electron-groups** are regions with high e^- density (lone pairs or bonds) around the central atom
  - The **electron-group arrangement** that minimizes the repulsion depends on the number of electron-groups that repel each other:

2	3	4	5	6
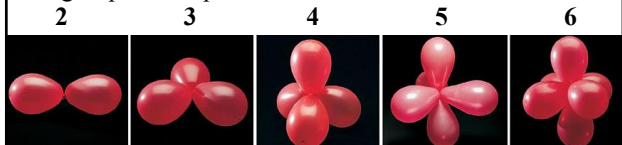
- The five most common **electron-group arrangements** and their characteristic angles:

LINEAR 180° TRIGONAL PLANAR 120° TETRAHEDRAL 109.5°

TRIGONAL BIPYRAMIDAL 90° 120° OCTAHEDRAL 90° 90°

  - **Both** bonding and nonbonding e^- groups are considered in the **electron-group arrangement**
  - **Only** the bonding e^- groups are considered in the **molecular shape** since they determine the positions of the atoms (lone pairs are ignored)
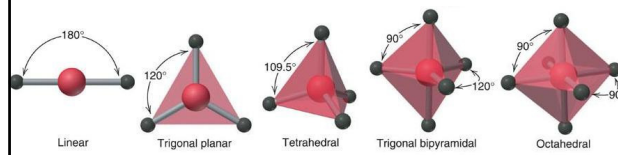- **VSEPR classes** – representations in the form AX_mE_n , where **A** is the central atom, **X** is an atom attached to it, and **E** is a nonbonding group (lone pair)
  $\Rightarrow$ *n* is the number of non-bonding groups (lone pairs) and *m* is the number of bonding groups (atoms attached to the central atom)
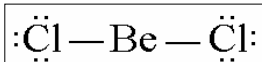

A = ⬤   X = ⬤

E =
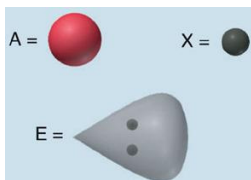
- VSEPR classes AX_2, AX_3, AX_4, AX_5 & AX_6
  - All electron-groups surrounding the central atom are **bonding groups**
  - If all surrounding atoms (**X**) are the same, the **bond angles** are equal to the characteristic angles of the arrangement
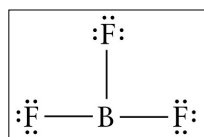 - The **molecular shape** and electron-group arrangement have the same name:

180° 120° 109.5° 90° 120° 90° 90°

Linear   Trigonal planar   Tetrahedral   Trigonal bipyramidal   Octahedral

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Examples:

Class	Shape
AX_2	Linear

Examples: CS_2, HCN, BeF_2

$:\ddot{C}l — Be — \ddot{C}l:$

Linear shape, bond angle of 180°

Class	Shape
AX_3	Trigonal planar

Examples: SO_3, BF_3, NO_3^-, CO_3^{2-}

$:\ddot{F}:$
$:\ddot{F} — B — \ddot{F}:$

Trigonal planar shape, bond angles of 120°

Examples:

Class	Shape
AX_4	Tetrahedral

Examples: CH_4, $SiCl_4$, SO_4^{2-}, ClO_4^-

$H — C — H$ with H above and below
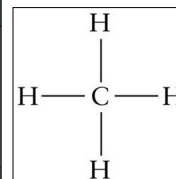
Tetrahedral shape, bond angles of 109.5°

Class	Shape
AX_5	Trigonal bipyramidal

Examples: PF_5, AsF_5, SOF_4

$:\ddot{C}l:$
$:\ddot{C}l — P — \ddot{C}l:$
$:\ddot{C}l$ $\ddot{C}l:$
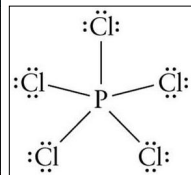
Trigonal bipyramidal shape, bond angles of 120 and 90°

• The VSEPR model treats multiple bonds in the same way as single bonds (a single bonding electron-group)

Example: CO_3^{2-}

$$\left[\begin{matrix} :\ddot{O}: \\ \| \\ :\ddot{O} - C - \ddot{O}: \end{matrix} \right]^{2-}$$
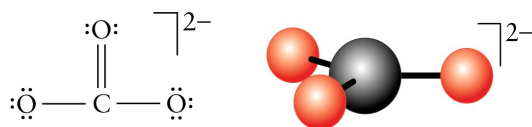
→**Three** atoms attached to a central atom (AX_3) → **Trigonal planar shape,** bond angles of 120°
→Any one of the resonance structures can be used to predict the molecular shape

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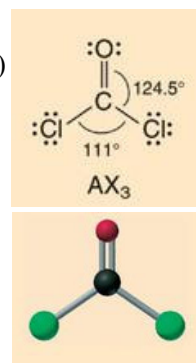• The effect of **double bonds** on **bond angles**

Example: Cl_2CO

→**Three** atoms attached to the central atom, no lone pairs (AX_3)
⇒**Trigonal-planar shape**
→The **bond angles deviate** from the ideal values
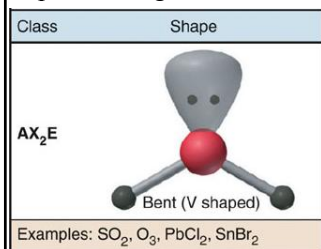→The double bond has greater **e⁻** density and repels the single bonds stronger
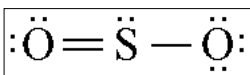⇒∠ Cl-C-Cl < 120°
∠ Cl-C-O > 120°

• **Trigonal planar** electron-group arrangement with **one lone pair**
→**Two** atoms attached to the central atom + **one** lone pair (AX_2E) → **Bent shape**
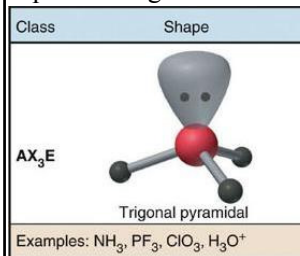→The **lone pair is bulkier** and repels the bonding pairs stronger → **bond angle is less than 120°**

Class	Shape
AX_2E	Bent (V shaped)
Examples: SO_2, O_3, $PbCl_2$, $SnBr_2$	

Example: SO_2

$$:\ddot{O} = \ddot{S} - \ddot{O}:$$
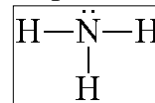
Bent shape
Bond angle of ~119°

• **Tetrahedral** electron-group arrangement with **one lone pair**
→**Three** atoms attached to the central atom + **one** lone pair (AX_3E) → **Trigonal pyramidal shape**
→The **lone pair is bulkier** and repels the bonding pairs stronger → **bond angles are less than 109.5°**

Class	Shape
AX_3E	Trigonal pyramidal
Examples: NH_3, PF_3, ClO_3, H_3O^+	

Example: NH_3

$$H - \ddot{N} - H$$
$$\quad | \quad$$
$$\quad H \quad$$

Trigonal pyramidal shape
Bond angle of 107.3°

• **Tetrahedral** electron-group arrangement with **two lone pairs**
→**Two** atoms attached to the central atom + **two** lone pairs (AX_2E_2) → **Bent shape**
→The **two lone pairs** have even greater repelling effect → **bond angles are less than 109.5°**

Class	Shape
AX_2E_2	Bent (V shaped)
Examples: H_2O, OF_2, SCl_2	

Example: H_2O

$$H - \ddot{O} - H$$
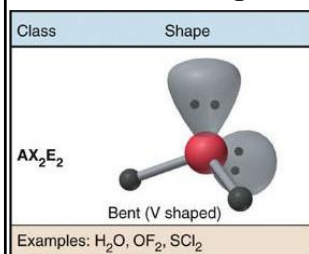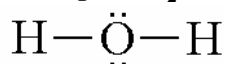
Bent shape
Bond angle of 104.5° (lower than in NH_3)

• Strengths of electron group repulsions
lone pair-lone pair > lone pair-bonding pair > bonding pair-bonding pair
⇒In the electron arrangement, lone pairs occupy positions as far from one another and from bonding pairs as possible

• **Trigonal bipyramidal** electron-group arrangement with **1**, **2** or **3 lone pairs**
– VSEPR classes AX_4E, AX_3E_2 and AX_2E_3
– The **lone pairs occupy** *equatorial* **positions** (provides more space for the lone pairs and minimizes the repulsion)

Top-left panel:

AX₄E — Seesaw
Examples: SF_4, XeO_2F_2, IF_4^+, $IO_2F_2^-$

AX₂E₃ — Linear
Examples: XeF_2, I_3^-, IF_2^-

AX₃E₂ — T-shaped
Examples: ClF_3, BrF_3

Axial positions

Equatorial positions

Top-right panel:
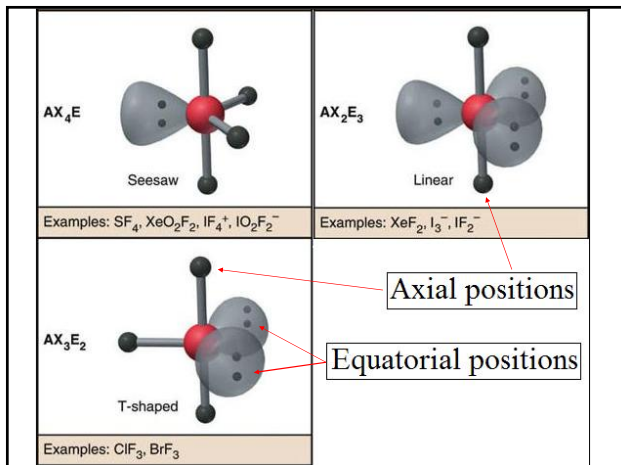
- **Octahedral** electron-group arrangement with **1** or **2 lone pairs**
  - VSEPR classes AX_5E, and AX_4E_2
  - The **lone pairs occupy positions opposite to each other** (provides the lowest repulsion)

AX₅E — Square pyramidal
Examples: BrF_5, TeF_5^-, $XeOF_4$

AX₄E₂ — Square planar
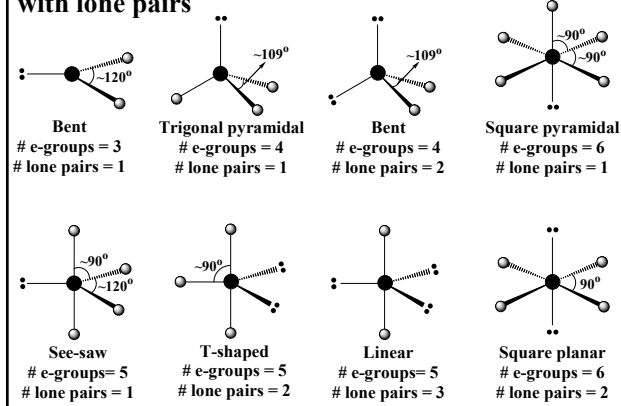Examples: XeF_4, ICl_4^-

Middle-left panel:
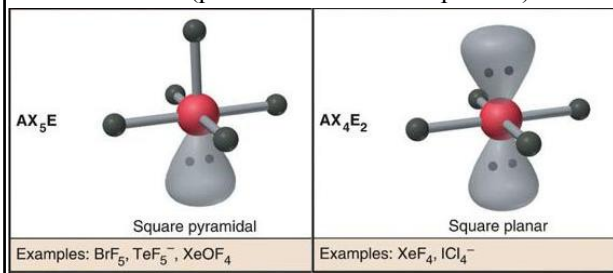
Summary of molecular shapes for central atoms with lone pairs

|			
Bent	Trigonal pyramidal	Bent	Square pyramidal
~120°	~109°	~109°	~90° / ~90°
# e-groups = 3	# e-groups = 4	# e-groups = 4	# e-groups = 6
# lone pairs = 1	# lone pairs = 1	# lone pairs = 2	# lone pairs = 1
See-saw	T-shaped	Linear	Square planar
~90° / ~120°	~90°		~90°
# e-groups = 5	# e-groups = 5	# e-groups = 5	# e-groups = 6
# lone pairs = 1	# lone pairs = 2	# lone pairs = 3	# lone pairs = 2

Middle-right panel:

- **Steps** in determining molecular shapes using the VSEPR model:
  - Write the Lewis structure
  - Determine the electron-group arrangement, ideal bond angles and VSEPR class
  - Place the surrounding atoms and lone pairs in appropriate positions around the central atom and predict any deviations from the ideal bond angles
  - Name the molecular shape
- For molecules with **more than one central atom**, find the electron-group arrangement and corresponding shape around each central atom (one central atom at a time)

Bottom-left panel:

Example: Determine the electron arrangement and molecular shape of I_3^-.
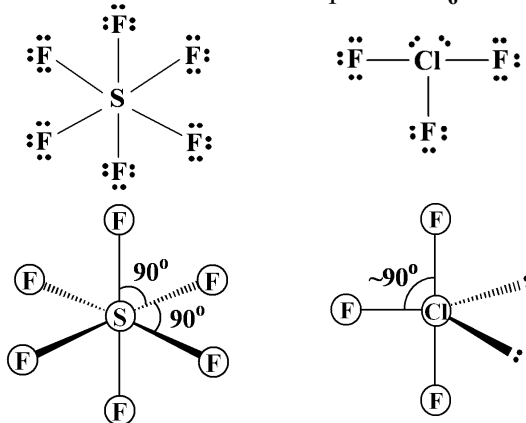
1. Lewis structure →
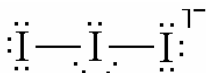
2. El-group arrangement → **trigonal bipyramidal** (**2** bonded atoms + **3** lone pairs = **5**), VSEPR class AX_2E_3
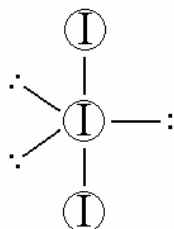
3. Lone pairs in equatorial positions, atoms in axial positions (**180°** bond angle)

4. Molecular shape → **linear**

Bottom-right panel:

Example: Determine the shapes of SF_6 and ClF_3

90° 90°

~90°

10.3 Charge Distribution in Molecules

**Bond Polarity and Molecular Polarity**

- **Polar covalent bonds** (due to unequal sharing of the bonding electrons) → **bond dipoles**
- **Dipole moment** (μ) – a measure of the magnitude and direction of a dipole
  - μ increases with increasing the partial charges of the atoms (Q) and the bond distance (r) → $\mu = Q \cdot r$
  - The direction of μ is from plus to minus
  - SI units → **C·m**
  - Other units → **debye (D) 1 D = 3.336×10^{-30} C·m**

- **Molecular dipole moment** (associated with the molecule as a whole) – can be represented as a sum of the bond dipoles of all bonds
- **Nonpolar** molecules – zero dipole moment
  - Homonuclear diatomic molecules (H_2, O_2, F_2, ...)
  - Polyatomic molecules where the bond dipoles cancel each other

  CO_2 is nonpolar – the bond dipoles of the C–O bonds cancel due to the linear shape

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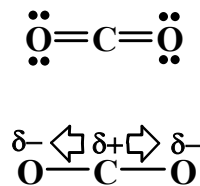
- **Polar** molecules – nonzero dipole moment
  - Heteronuclear diatomic molecules (**HF**, **CO**, ...)
  - Polyatomic molecules where the bond dipoles do not cancel each other
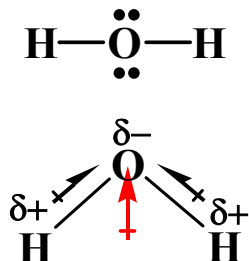
H_2O is a polar molecule because the bond dipoles of the O-H bonds do not cancel due to the bent molecular shape

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⇒ The polarity of molecules depends on both the polarity of the bonds and the molecular geometry which must be known

Example: The isomers 1,2-dichlorobenzene and 1,4-dichlorobenzene have the same formula, $C_6H_4Cl_2$, but different physical properties

| Polar	Non-polar
B.p. 180°C	B.p. 174°C
Very soluble in EtOH	Slightly soluble in EtOH
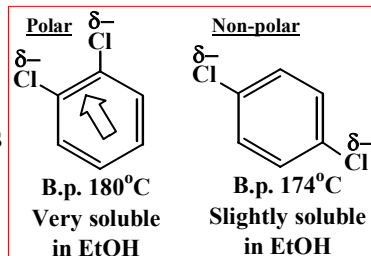
- Highly symmetric molecules are normally nonpolar
  - AX_n molecules (n=2, 3, 4, 5, 6) where **X** are atoms of the same element
  - Molecules with symmetrically positioned lone pairs (AX_2E_3, AX_4E_2)
- Molecules with asymmetrically positioned lone pairs or different atoms attached to the central atom are normally polar
  - AX_2E, AX_2E_2, AX_3E, AX_3E_2, AX_4E, AX_5E, …
  - CF_3H, CF_2H_2, SO_2(bent), ...

Example: Is PCl_2F_3 a polar molecule?

1. The Lewis structure is similar to PCl_5 (five atoms bonded to the **P** atom, no lone pairs)
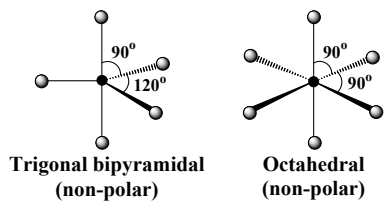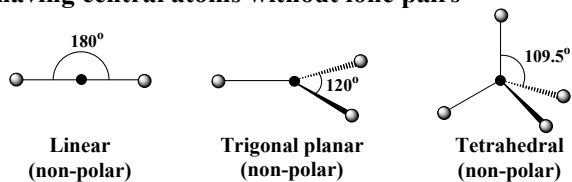
⇒ **trigonal bipyramidal shape**

2. The **Cl** atoms are larger and take two of the equatorial positions; the **F** atoms are smaller and take the two axial and one of the equatorial positions
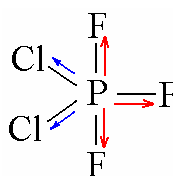
The P–F dipoles are larger than the P–Cl dipoles (ΔEN is larger for **P** and **F**)

The molecule is **polar** – the bond dipoles don't cancel (asymmetric arrangement)

Summary of molecular polarities for molecules having central atoms without lone pairs

180°

**Linear
(non-polar)**

120°

**Trigonal planar
(non-polar)**

109.5°

**Tetrahedral
(non-polar)**

90°
120°

**Trigonal bipyramidal
(non-polar)**

90°
90°

**Octahedral
(non-polar)**

Summary of molecular polarities for molecules having central atoms with lone pairs

~120°

**Bent
(polar)**

~109°

**Trigonal pyramidal
(polar)**

~109°

**Bent
(polar)**

~90°
~90°

**Square pyramidal
(polar)**

~90°
~120°

**See-saw
(polar)**

~90°

**T-shaped
(polar)**

**Linear
(non-polar)**

90°

**Square planar
(non-polar)**