

Gases and the Kinetic Molecular Theory

- Importance in atmospheric phenomena, gas phase reactions, combustion engines, etc.

5.1 The Physical States of Matter

- The condensed states – liquid and solid
- The gaseous state
 - Gas volume changes greatly with pressure
 - Gas volume changes greatly with temperature
 - Gases have low viscosity (flow easily)
 - Gases have low density (~1000 times lower than liquids and solids)
 - Gases are miscible in all proportions

- Molecular model of the gaseous state
 - Molecules are in constant, rapid, random motion (explains the absence of definite shape, miscibility, low viscosity)
 - Molecules are widely separated (explains the absence of definite volume, low density, compressibility)

5.2 Pressure

- Gas molecules collide with each other and the walls of the container → molecules exert force on the walls

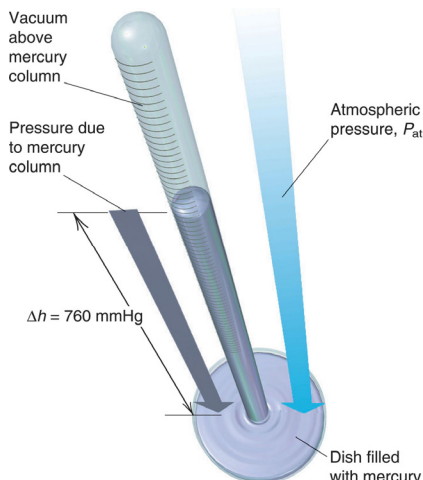
$$\text{Pressure} = \frac{\text{Force}}{\text{Area}}$$

$$P = \frac{F}{A}$$

- **Atmospheric pressure (P_{atm})** – caused by the gravitational pull of the Earth → molecules exert force on all objects

➤ Barometers - measure the atmospheric pressure (Torricelli)

- no pressure above the mercury column (vacuum)
- the weight of the Hg column balances P_{atm}
- the height of the Hg column is proportional to P_{atm}



g - acceleration of free fall (**9.81 m/s²**)
 d - density of Hg (**13546 kg/m³**)
 V - volume of Hg column
 h - height of Hg column (**0.760 m** at sea level)
 A - area of Hg column base

$$P_{atm} = P_{Hg} = \frac{F}{A} \qquad F = m_{Hg}g$$

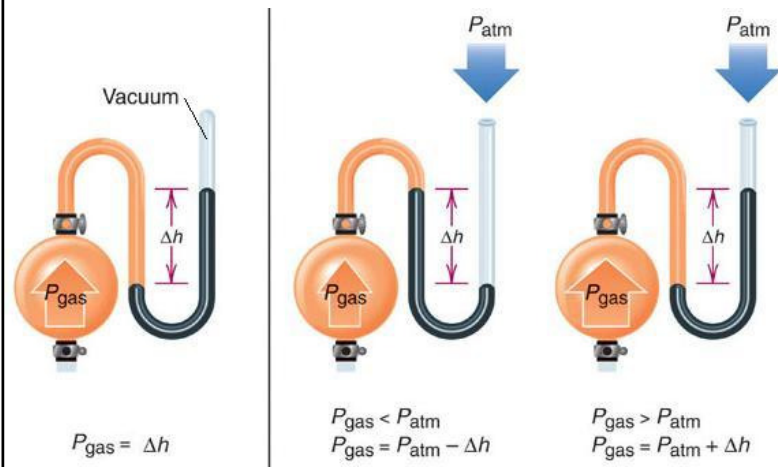
$$m_{Hg} = dV = dhA \quad \Rightarrow \quad F = dhAg$$

$$\Rightarrow P_{atm} = \frac{dhAg}{A} = dhg$$

$$P_{atm} = 13546 \times 0.760 \times 9.81 = 1.01 \times 10^5 \text{ kg} / \text{m} \cdot \text{s}^2$$

➤ **Manometers** – measure the pressure of gases in containers

- **Close-end** and **open-end** manometers



Units of Pressure

- SI unit → pascal (Pa)

$$1 \text{ Pa} = 1 \text{ N/m}^2 = 1 \text{ kg/m} \cdot \text{s}^2$$

$$P_{atm} = 1.01 \times 10^5 \text{ Pa} \quad (\text{at sea level})$$

- Conventional units:

$$\text{atm} \rightarrow 1 \text{ atm} = 101325 \text{ Pa} \quad (\text{exactly})$$

$$\text{bar} \rightarrow 1 \text{ bar} = 100000 \text{ Pa} \quad (\text{exactly})$$

$$\text{torr} \rightarrow 760 \text{ Torr} = 1 \text{ atm} \quad (\text{exactly})$$

$$\text{mm Hg} \rightarrow 1 \text{ mmHg} = 1 \text{ Torr}$$

$$\text{lb/in}^2 \rightarrow 14.7 \text{ lb/in}^2 = 1 \text{ atm}$$

Example:

Convert **630.0 Torr** to atmospheres and kilopascals.

$$630.0 \text{ Torr} \times \left(\frac{1 \text{ atm}}{760 \text{ Torr}} \right) = 0.8289 \text{ atm}$$

$$630.0 \text{ Torr} \times \left(\frac{1 \text{ atm}}{760 \text{ Torr}} \right) \times \left(\frac{101325 \text{ Pa}}{1 \text{ atm}} \right) = 8.399 \times 10^4 \text{ Pa} = 83.99 \text{ kPa}$$

5.3 The Gas Laws

- Relate the parameters of the gaseous state – pressure, volume, temperature, and number of moles

Boyle's Law

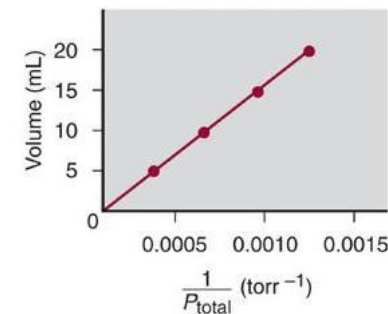
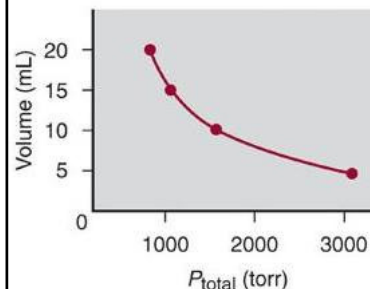
- At constant temperature (T) the pressure (P) of a fixed amount of gas is inversely proportional to its volume (V)

⇒ At constant T and n :

$$P = \frac{k}{V} \quad k \rightarrow \text{constant (depends on } T \text{ and } n)$$

$$PV = k = \text{constant} \quad V \downarrow \Leftrightarrow P \uparrow$$

| V (mL) | P (torr) | $\frac{1}{P}$ | PV (torr • mL) |
|----------|------------|---------------|---------------------|
| 20.0 | 780 | 0.00128 | 1.56×10^4 |
| 15.0 | 1038 | 0.000963 | 1.56×10^4 |
| 10.0 | 1560 | 0.000641 | 1.56×10^4 |
| 5.0 | 3112 | 0.000321 | 1.56×10^4 |



- Assume two states of a gas at constant T

– state 1 → P_1, V_1

– state 2 → P_2, V_2

$$P_1 V_1 = k \quad P_2 V_2 = k$$

$$P_1 V_1 = P_2 V_2$$

Example: A 2.0 L sample of oxygen at 10 atm is transferred to a 15.0 L container at constant temperature. What is the new pressure?

$$V_1 = 2.0 \text{ L} \quad P_1 = 10 \text{ atm} \quad V_2 = 15.0 \text{ L} \quad P_2 = ?$$

$$P_2 = \frac{P_1 V_1}{V_2} = \frac{10 \text{ atm} \times 2.0 \text{ L}}{15.0 \text{ L}} = 1.3 \text{ atm}$$