

- **Derived units** (derived from the base units)

- **Volume ( $V$ )**  $\rightarrow 1 \text{ m}^3 = (1 \text{ m}) \times (1 \text{ m}) \times (1 \text{ m})$

$$1 \text{ mL} = 1 \text{ cm}^3 = (1 \text{ cm}) \times (1 \text{ cm}) \times (1 \text{ cm}) = (10^{-2} \text{ m}) \times (10^{-2} \text{ m}) \times (10^{-2} \text{ m}) = (10^{-2} \times 10^{-2} \times 10^{-2}) \text{ m}^3 = 10^{-6} \text{ m}^3$$

$$1 \text{ L} = 1 \text{ dm}^3 = 10^{-3} \text{ m}^3 \qquad 1 \text{ mL} = 10^{-3} \text{ L}$$

- **Density ( $d$ )**  $\rightarrow$  mass ( $m$ ) per unit volume ( $V$ )  
 $\rightarrow (d = m/V)$

$$\text{unit of } d = (1 \text{ kg}) / (1 \text{ m}^3) = 1 \text{ kg/m}^3$$

- **Velocity ( $v$ )**  $\rightarrow$  distance ( $l$ ) per unit time ( $t$ )  
 $\rightarrow (v = l/t)$

$$\text{unit of } v = (1 \text{ m}) / (1 \text{ s}) = 1 \text{ m/s}$$

- **Extensive properties** – depend on sample size (mass, volume, length, ...)

- **Intensive properties** – independent of sample size (density, temperature, color, ...)

**Example:**

What is the density of an alloy in  $\text{g/cm}^3$ , if **55 g** of it displace **9.1 mL** of water?

$$d = m/V = (55 \text{ g}) / (9.1 \text{ mL}) = 6.0 \text{ g/mL} = 6.0 \text{ g/cm}^3$$

**Example:**

- Convert the density of gold, **19.3  $\text{g/cm}^3$** , to  **$\text{kg/m}^3$** .

$\Rightarrow$  need to convert both the numerator and denominator **g**  $\rightarrow$  **kg** and  **$\text{cm}^3$**   $\rightarrow$   **$\text{m}^3$**

$$1 \text{ kg} = 10^3 \text{ g}$$

$$1 \text{ cm} = 10^{-2} \text{ m} \Rightarrow 1 \text{ cm}^3 = (10^{-2})^3 \text{ m}^3 = 10^{-6} \text{ m}^3$$

$$d = 19.3 \frac{\cancel{\text{g}}}{\cancel{\text{cm}^3}} \times \left( \frac{1 \text{ kg}}{10^3 \cancel{\text{g}}} \right) \times \left( \frac{1 \cancel{\text{cm}^3}}{10^{-6} \text{ m}^3} \right) = 19.3 \times 10^3 \frac{\text{kg}}{\text{m}^3}$$

**Example:**

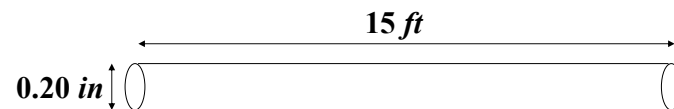
What is the mass in **kg** of a **15 ft** wire made of an alloy with  **$d = 6.0 \text{ g/cm}^3$**  if the diameter of the wire is **0.20 in**?

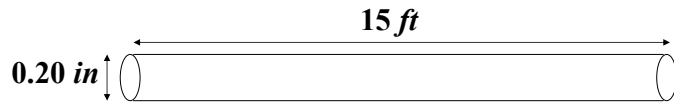
**Plan:**

Diameter  $\rightarrow$  radius (cm)  $\rightarrow$  cross-section area ( $\text{cm}^2$ )

Length (cm)  $\times$  cross-section area  $\rightarrow$  volume ( $\text{cm}^3$ )

Volume & density  $\rightarrow$  mass (g)  $\rightarrow$  mass (kg)





$$\text{Radius} \rightarrow r = 0.20 \text{ in} / 2 = 0.10 \text{ in}$$

$$r = 0.10 \text{ in} \times \left( \frac{2.54 \text{ cm}}{1 \text{ in}} \right) = 0.254 \text{ cm}$$

$$A = \pi r^2 = 3.14 \times (0.254 \text{ cm})^2 = 0.203 \text{ cm}^2$$

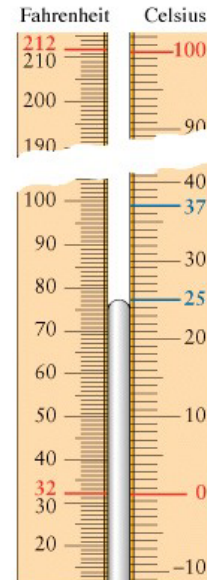
$$l = 15 \text{ ft} \times \left( \frac{12 \text{ in}}{1 \text{ ft}} \right) \times \left( \frac{2.54 \text{ cm}}{1 \text{ in}} \right) = 457 \text{ cm}$$

$$V = l \times A = 457 \text{ cm} \times 0.203 \text{ cm}^2 = 92.7 \text{ cm}^3$$

$$m = 92.7 \text{ cm}^3 \times \left( \frac{6.0 \text{ g}}{1 \text{ cm}^3} \right) \times \left( \frac{1 \text{ kg}}{1000 \text{ g}} \right) = 0.56 \text{ kg}$$

- **Temperature ( $T$ )** – a measure of how hot or cold an object is relative to other objects
  - $T$  reflects the thermal energy of the object
  - $T$  is an intensive property
- **Heat** – the flow of thermal energy between objects
  - Heat flows from objects with higher  $T$  to objects with lower  $T$
  - Heat is an extensive property
  - Heat and temperature are different
- **Thermometers**
  - Used to measure  $T$

- The **Celsius** scale
    - $0^\circ\text{C}$  → freezing point of water
    - $100^\circ\text{C}$  → boiling point of water
  - The **Fahrenheit** scale
    - $0^\circ\text{F}$  → freezing point of salt/water mixture
    - $100^\circ\text{F}$  → body temperature
    - water freezes at  $32^\circ\text{F}$  and boils at  $212^\circ\text{F}$
- ⇒ 100 Celsius degrees ↔ 180 Fahrenheit degrees



$$\left( \frac{180^\circ\text{F}}{100^\circ\text{C}} \right) = \left( \frac{9^\circ\text{F}}{5^\circ\text{C}} \right)$$

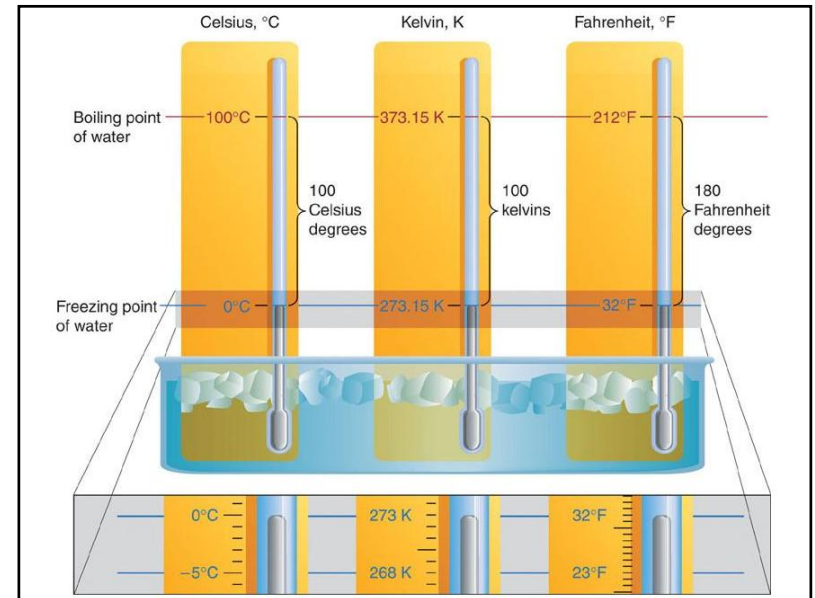
$$T^\circ\text{F} = \left( \frac{9^\circ\text{F}}{5^\circ\text{C}} \right) T^\circ\text{C} + 32^\circ\text{F}$$

$$T^\circ\text{C} = \left( \frac{5^\circ\text{C}}{9^\circ\text{F}} \right) (T^\circ\text{F} - 32^\circ\text{F})$$

- The **Kelvin** scale - absolute temperature scale
    - 0 K → lowest possible temperature
    - 0 K = -273.15°C
    - same size of degree unit as Celsius
- ⇒ water freezes at 273.15 K and boils at 373.15 K

- $T \text{ K} = T^{\circ}\text{C} + 273.15$

- $T^{\circ}\text{C} = T \text{ K} - 273.15$



### Example:

- Convert -40°F in °C and K.
- $T^{\circ}\text{C} = (5^{\circ}\text{C}/9^{\circ}\text{F}) \times [-40^{\circ}\text{F} - 32^{\circ}\text{F}] =$   
 $= (5/9) \times (-72)^{\circ}\text{C} = -40^{\circ}\text{C}$
- $T \text{ K} = -40^{\circ}\text{C} + 273.15 = 233 \text{ K}$